

The First Derivative Test is used to:

- Determine the sections of the graph of  $f(x)$  that are increasing or decreasing
- Identify extreme values (max/min)

Steps

- ① Find  $f'(x)$
- ② Identify the critical points (set  $f'(x)$  equal to zero and solve for  $x$ )
- ③ Set up a table:

Interval	create intervals using the critical points
Test Value	pick a # in each interval
$f'(x) =$	plug each TV into $f'(x)$ to find +/- sign
Inc/Dec	+ INC      - DEC

- ④ Draw a rough sketch of the INC/DEC intervals and determining extreme values

ex  $f(x) = x^4 - 8x^2 + 1$  [-4, 1]

①  $f'(x) = 4x^3 - 16x$   
 ②  $4x^3 - 16x = 0$   
 GCF  $4x(x^2 - 4) = 0$   
 DOTS  $4x(x+2)(x-2) = 0$

$4x(x+2)(x-2)$	
-3	- - - -> -
-1	- + - -> +
$\frac{1}{2}$	+ + - -> -

$x=0$   $x=-2$   $x=2$  ←  $x=2$  is not used because it is outside the given interval

③

Int.	$(-4, -2)$	$(-2, 0)$	$(0, 1)$
T.V.	-3	-1	$\frac{1}{2}$
$f'(x) =$	-	+	-
I/D	DEC	INC	DEC

